

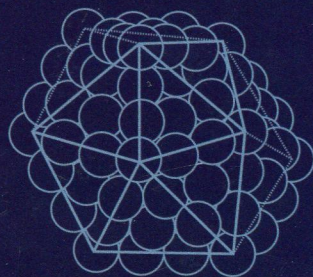
Second Edition

# Crystallography and Crystal Defects



Anthony Kelly and Kevin M. Knowles

 WILEY



# Crystallography and Crystal Defects

Second Edition

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