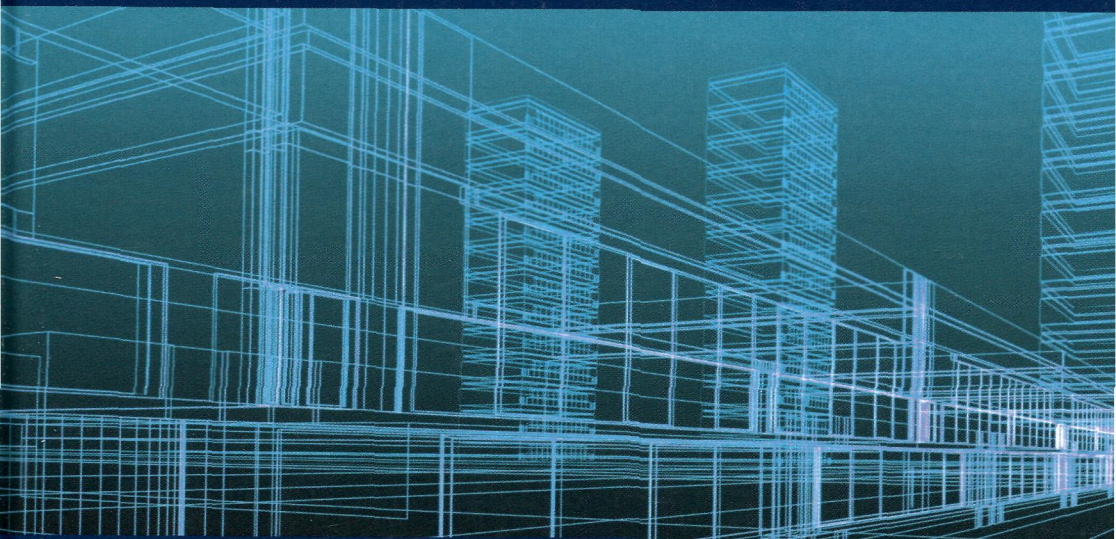


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Uncertainty and Optimization in Structural Mechanics

Abdelkhalak El Hami and Bouchaïb Radi

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