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*Editors*

# Optical Properties of 3d-Ions in Crystals

Spectroscopy and Crystal Field Analysis



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# **Optical Properties of 3d-Ions in Crystals: Spectroscopy and Crystal Field Analysis**

With 64 figures



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