

DE GRUYTER

*Michael V. Sadovskii*

# STATISTICAL PHYSICS

2ND EDITION

TEXTS AND MONOGRAPHS  
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Michael V. Sadovskii

# Statistical Physics

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