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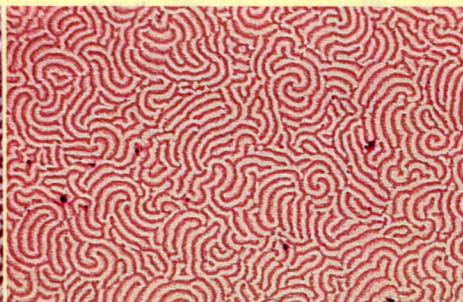
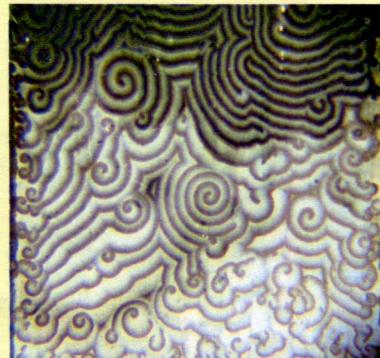


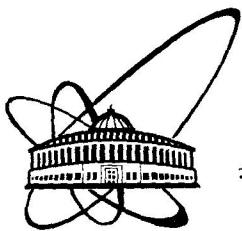
Nucleation Theory and Applications

Edited by Jürg W. P. Schmelzer

Gerd Röpke

Vyatcheslav B. Priezzhev





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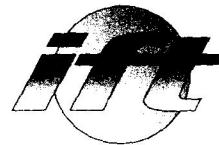


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The present book consists of contributions directed to the analysis of first- and second-order phase transitions from both experimental and theoretical points of view. They have been presented and discussed in the course of the research workshops «Nucleation Theory and Applications» organized at the Bogoliubov Laboratory of Theoretical Physics of the Joint Institute for Nuclear Research in Dubna, Russia, in the period from 2006 to 2008. The volume of the proceedings supplements results published in three former conference proceedings in the years 1999, 2002 and 2005 also in Dubna and two monographs with overview lectures published by WILEY-VCH in 1999 and 2005. In the present proceedings, the spectrum of different topics includes experimental investigations of thermodynamic properties of matter (in thermodynamic equilibrium and non-equilibrium states including glasses), nucleation-growth phenomena and their theoretical interpretation, the theoretical analysis of the course of first- and second-order phase transitions, the discussion of principal problems of the thermodynamic description of clusters, molecular-dynamic analyses of phase equilibria and clustering phenomena, and a variety of applications.

Теория нуклеации и ее применения / Под ред. Ю. Шмельцера, Г. Рёпке,
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В сборнике представлены результаты экспериментального и теоретического анализа фазовых превращений первого и второго рода, которые докладывались и обсуждались на рабочих совещаниях «Теория нуклеации и ее применения», проходивших в Лаборатории теоретической физики им. Н. Н. Боголюбова Объединенного института ядерных исследований в 2006–2008 гг. Эти результаты дополняют данные, опубликованные в трех предыдущих томах серии, вышедших в свет в 1999, 2002 и 2005 гг. в Дубне, и двух монографиях, изданных в 1999 и 2005 гг. издательством WILEY-VCH. Сборник состоит из 25 разделов, в которых отражены результаты экспериментального анализа свойств веществ (в термодинамически равновесных и неравновесных состояниях, включая стекла), процессов нуклеации и роста кластеров новых фаз и теоретическая интерпретация этих данных, общий теоретический анализ фазовых превращений первого и второго рода, обсуждаются принципиальные вопросы термодинамического описания кластеров, молекулярно-динамического анализа фазовых равновесий и процессов агрегации, а также рассматриваются разнообразные применения теории.

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Contents

1	Introductory Remarks	1
2	Classical and Generalized Gibbs' Approaches and the Properties of Critical Clusters in Nucleation Theory	
	<i>Jürg W. P. Schmelzer</i>	
	<i>Institut für Physik, Universität Rostock, Universitätsplatz, 18051 Rostock, Germany</i>	3
2.1	Introduction	3
2.2	Generalized Gibbs' Approach and the Work of Critical Cluster Formation	4
2.3	The Temperature of the Critical Clusters	5
2.3.1	The Problem	5
2.3.2	Results of MD-simulations	7
2.3.3	Interpretation in Terms of the Generalized Gibbs' Approach	7
2.4	Discussion	9
3	On the Thermodynamic Properties of Metastable Systems	
	<i>Vladimir G. Baidakov</i>	
	<i>Institute of Thermal Physics, Ural Branch of the Russian Academy of Sciences, 620016 Ekaterinburg, Amundsen Str. 106, Russia</i>	11
3.1	Introduction	11
3.2	Effect of Fluctuations on the Thermodynamic Properties of a System: General Considerations	11
3.3	Effect of Fluctuations on the Thermodynamic Properties of a System: An Example	13
3.4	Discussion	15
4	Nanoscale Structure of the Liquid–Gas Interphase Surface and the Capillary Fluctuations	
	<i>Dmitry I. Zhukhovitskii</i>	
	<i>Joint Institute of High Temperatures, Russian Academy of Sciences, Izhorskaya 13/19, 125412 Moscow, Russia</i>	17
4.1	Introduction	17
4.2	Simulation Procedure	19
4.3	Definition of the Cluster Surface	21
4.3.1	Definition of a Bond	21
4.3.2	Cluster Particles Classification	22
4.3.3	Calculation of the Number of Bonds for a Cluster with Arbitrary Size	25
4.4	Wave Number Fourier Spectrum of Surface Fluctuations	26
4.4.1	Cluster Slice Spectra from MD Simulation	26
4.4.2	Capillary Fluctuations of a Planar Liquid–Gas Interphase Surface	29
4.4.3	Capillary Fluctuations of the Cluster Surface	31
4.4.4	Other Estimates for the Surface Variance	32
4.5	Frequency Fourier Spectrum	34
4.6	Average Density Distribution	36

4.7 Conclusions	38
5 Method of Direct Numerical Solution for Simulation of Supersaturated Vapor Condensation	
<i>Naoum M. Kortsensteyn⁽¹⁾ and Arsenij K. Yastrebov⁽²⁾</i>	
(¹) <i>Krzhizhanovsky Power Engineering Institute, Leninskij pr. 19, 119991 Moscow, Russia</i>	
(²) <i>Moscow Power Engineering Institute (Technical University), Krasnokazarmennaya ul. 14, 111250 Moscow, Russia</i>	
5.1 Introduction	41
5.2 Method of Direct Numerical Solution	43
5.3 Formulation of the Relaxation Problem	45
5.4 Results of Calculations and Discussion	47
5.4.1 Free-molecular Regime of Droplet Growth	47
5.4.2 Transitional Regime of Droplet Growth	49
5.4.3 Dependence of the Saturation Pressure on Droplet Radius	51
5.5 Conclusions	54
6 On the Condensation-Ionization Instability in Aerosol Plasmas	
<i>Naoum M. Kortsensteyn and Eugene V. Samuilov</i>	
<i>Krzhizhanovsky Power Engineering Institute, Leninskij pr. 19, 119991 Moscow, Russia</i>	
6.1 Introduction	57
6.2 Properties of Explosion Products	58
6.3 Formation of Condensation Aerosol	62
6.3.1 Schema of the Condensation Process	62
6.3.2 Set of Equations	62
6.3.3 Inclusion of Heterogeneous Condensation and Brownian Coagulation	63
6.3.4 Calculation Results	64
6.3.5 Effect of Non-Evaporated Droplets on the Process of Bulk Condensation	65
6.3.6 Calculation of $n_d r_d$ and $n_d r_d^3(g_{MgO})$	66
6.4 Ionisation of Condensation Aerosol	67
6.4.1 Calculation of the Electron Concentration	67
6.4.2 Inclusion of the Ionic Nucleation	70
6.5 Conclusions	71
7 Decay of Metastable States: Nucleation Initiated by Transitions of Already Formed Embryos	
<i>Victor B. Kurasov</i>	
<i>St. Petersburg State University, Department Computational Physics, 198904 St. Petersburg, Petrodvorets, Russia</i>	
7.1 Introduction	73
7.2 Qualitative Description	73
7.3 Effective Source	74
7.4 Secondary Nucleation	75
7.5 Approximation for $S(x)$	76
7.6 Nucleation at Small and Intermediate D -Values	77
7.7 Nucleation at Large D -Values	78
7.8 Concluding Remarks	79
8 Non-Steady Theory of Heat Effects at Droplet Diffusional Growth	
<i>Alexander P. Grinin, Gennady Yu. Gor, and Fedor M. Kuni</i>	
<i>St. Petersburg State University, Institute of Physics, 198504 St. Petersburg, Petrodvorets, Ulyanovskaya st. 1, Russia</i>	
	81

8.1	Introduction	81
8.2	Non-steady Vapour Concentration Profile around the Droplet Growing in Diffusion Regime	82
8.3	Non-steady Temperature Profile around the Droplet Growing in Diffusion Regime	86
8.4	Approximation of High Density of the Liquid in the Droplet	88
8.5	Strong Display of Condensation Heat Release Effects	90
8.6	Weak Display of Condensation Heat Release Effects	92
9	Possible Mechanisms of Pattern Formation in Plasma Melting of Glasses: Coupling of Melting and Flow Processes, Oscillations, Rayleigh-Taylor and Convective Instabilities	
	<i>Alexander L. Tseskis⁽¹⁾, Naoum M. Kortsenstein⁽²⁾, and Jürg W. P. Schmelzer⁽³⁾</i>	
	⁽¹⁾ <i>Am Weidenbusch 29, 51381 Leverkusen, Germany</i>	
	⁽²⁾ <i>Krzhizhanovsky Power Engineering Institute, Leninskij Prospekt 19, 117927 Moscow, Russia</i>	
	⁽³⁾ <i>Institute of Physics, University of Rostock, 18051 Rostock, Germany</i>	97
9.1	Introduction	97
9.2	Structure Formation in Coupled Melting and Flow	99
9.3	Structure Formation in Oscillating Fluids	99
9.4	The Rayleigh-Taylor Instability	100
9.4.1	Basic Mechanism	100
9.4.2	Rayleigh's Original Approach	102
9.4.3	Extensions of Rayleigh's Theory	103
9.4.4	Rayleigh-Taylor Instability and Waves on Fluid Surfaces	103
9.5	Diffusive Convection	105
9.6	Conclusions	108
10	Crystallization of Quartz Glasses	
	<i>Victor K. Leko</i>	
	<i>OOO "Thermex", Srednij Prospekt 86, 199105 St. Petersburg, Russia</i>	109
10.1	Introduction	109
10.2	Literature Review	112
10.3	Development of Experimental Techniques	122
10.4	Basic Phenomenological Features of Crystallization Processes	124
10.5	Influence of the Degree of Silica Reduction	128
10.6	Influence of Concentration of "Structural Water"	132
10.7	Influence of Fusion Penetration Degree of Quartz or Cristobalite Particles on Crystallization of Quartz Glasses	136
10.8	Influence of Surface Contamination on Crystallization Kinetics	139
10.9	Influence of the Composition of the Gaseous Medium on Crystallization of Quartz Glass	141
10.9.1	Introductory Comments	141
10.9.2	On Crystallization in Dry Gas Media	141
10.9.3	Experiments on Crystallization in an Atmosphere Containing Water Vapor	143
10.9.4	Crystallization of Quartz Glasses in the Atmosphere of Gases in Equilibrium with the Melt	143
10.10	Influence of the Drawing Process on Crystallization of Tubes of Quartz Glasses	146
10.11	Discussion of the Results	151
10.11.1	Introductory Remarks	151
10.11.2	Influence of Surface Reactions on Crystallization	152
10.11.3	Relation between Crystallization Rate and Viscosity	155
10.12	Conclusions	162
11	Formation and Evolution of Bubbles in Silica Melts and Methods of Their Removal from the	

Melt	
Boris Z. Pevzner and Sergey V. Tarakanov	
Laboratory of Glass Properties, St-Petersburg, Russia	167
Part I: Experimental Data and Basic Mechanisms	167
11.1 Introduction	167
11.2 Sources of Bubbles in Silica Melt and in Silica Glass	168
11.2.1 Brief Information on the Technology of Silica Glass Production	168
11.2.2 Raw Materials as the Sources of Bubbles	169
11.2.3 The Furnace Atmosphere as a Source of Bubbles	171
11.2.4 Interaction of Heaters and Form-Shaping Equipment with the Melt as Source of Bubbles	172
11.2.5 Brief Report on the Concentrations of Impurities, Including Dissolved Gases, in Commercial Silica Glasses	173
11.2.6 Experimental Study of Formation and Evolution of Bubbles in Silica Melts	173
11.3 Physico-chemical Properties of Silica Melts Influencing the Formation and Evolution of Gas Bubbles	176
11.3.1 Surface Tension	176
11.3.2 Density	176
11.3.3 Viscosity	177
11.3.4 Solubility and Diffusion of Gases	178
11.4 Summary to Part I	186
Part II: Theoretical Consideration and Computer Simulation of the Process	187
11.5 Introduction to Part II	187
11.5.1 Main Stages of Fusion of Powdered Silica under Heating as well as the formation of the Bubble Structure	187
11.5.2 Selection of Parameters for the Temperature Dependence Equations that describe the Properties of the Silica Melt Affecting the Kinetics of the Process	188
11.6 Microrheological Model and Computer Simulation of the Process	189
11.6.1 The Microrheological Model of Sintering the Powder and Forming the Structure of a Porous Body	189
11.6.2 Influence of Some Technology Factors on Formation of Bubble Structure under Heating of Powdered Silica Glass: Computer Simulation of the Process	196
11.7 Summary to Part II	203
Part III: Mathematical Modeling and Computer Simulation of the Behavior of Gas-Filled Bubbles in Silica Melts	206
11.8 Introduction	206
11.9 Behavior of Isolated Bubbles	208
11.10 Behavior of Solitary Gas-Filled Bubbles under Mass Exchange with the Melt	209
11.11 Two-phase Approach to the Description of a Monodisperse Ensemble of Bubbles	211
11.12 Two-phase Approach to the Description of Polydisperse Ensembles of Bubbles	216
11.13 Diffusion of the Dissolved Gas in the Melt	219
11.14 Relative Motion of Bubbles in the Melt: Modification of the Mathematical Model	222
11.15 Flow of the Melt Governed by the Motion of the Bubbles: Complete System of Equations for Modeling of the Behavior of Gas-filled Bubble Ensembles in the Melt	226
11.16 Summary to Part III	229
12 Thermodynamics of Melting and the Formation of Glasses and Crystals	
Hans-Jürgen Hoffmann	
Technische Universität Berlin, Institute of Materials Science and Technology: Vitreous Materials, Englische Strasse 20, 10587 Berlin, Germany	235

12.1 Introduction	235
12.2 Analysis of the Enthalpy Functions of One-component Systems	237
12.2.1 Theoretical Preliminaries	237
12.2.2 Mono-atomic One-component Systems	239
12.2.3 Multi-atomic One-component Systems	242
12.3 Melting and the Glass Transformation	242
12.4 Effects Occurring in the Glass Transformation Range	244
12.5 What Makes Solids and Melts Expand?	245
12.6 Modulus of Compression of the Chemical Elements	250
12.7 Necessary Criteria for Glass Formation	250
12.8 Possible Extension to Multi-component Systems	253
12.9 Discussion	254
13 Phase and Glass Forming Diagrams and Crystallization Behavior of the BaO - TiO₂ - B₂O₃ Stoichiometric Glass Ceramics	
<i>Rafael M. Hovhannisyan, Hovakim A. Alexanyan, Hovsep Shirinyan, Bella V. Grigoryan and Berta V. Petrosyan</i>	
<i>Scientific-Production Enterprise of Material Science, 17 Charents street, 0025 Yerevan, Armenia</i>	257
13.1 Introduction	257
13.2 Experimental	258
13.3 Results	260
13.3.1 Glass Formation and Phase Diagrams	260
13.3.2 Crystallization Behavior of Stoichiometric Compositions in the BaO-TiO ₂ -B ₂ O ₃ system	263
13.4 Discussion	269
13.5 Conclusions	270
14 Adiabatic Nucleation in Devitrifying and Non-Devitrifying Oxide Glasses	
<i>Erich Meyer and Vitorvani Soares</i>	
<i>Instituto de Física da Universidade Federal do Rio de Janeiro, Bloco A - C.T., Cidade Universitária, 21945-970 Rio de Janeiro, Brazil</i>	273
14.1 Introduction	273
14.2 Basic Thermodynamics	274
14.3 Nucleation	275
14.4 Thermodynamics of the Nucleus	276
14.5 Diffusion and Viscosity	278
14.6 The Nucleation Frequency	281
14.7 Comparison with Experimental Data	281
14.8 Discussion and Conclusions	282
15 Fluctuation Theory Applied to Water Vapor Nucleation	
<i>Norberto Helil Pasqua and Bernhard Joachim Mokross</i>	
<i>Instituto de Física de São Carlos, Universidade de São Paulo, 13560-970, Caixa Postal 369, São Carlos-SP, Brazil</i>	285
15.1 Introduction	285
15.2 Nucleation Induced by Fluctuations: The Model	286
15.3 Preliminary Results	287
15.4 Conclusions and Application of Constant Pressure Ensemble to Fluctuation Theory	288
15.5 Appendices	289
15.5.1 Appendix A: Numerical Algorithm	289

15.5.2 Appendix B: Experimental Procedure and Data Analysis	291
16 Glass as a Solid Non-equilibrium Phase under Negative Pressure	
<i>Leonid M. Landa, Scott Thomsen, and Richard Hulme</i>	
<i>Guardian Industries Corporation, Science and Technology, 14511 Romine Road, Carleton, MI 48117, USA</i>	295
16.1 Introduction	295
16.2 Negative Pressure in a Glass-forming System	296
16.3 Excess Volume of Glass	296
16.4 Phase Transitions in the "Liquid → Glass" System	297
16.5 Absence of the Leap of Entropy in the Transition Point	299
16.6 Ehrenfest's Equation and Glass Transition of a Liquid	300
16.7 Sufficient Indicators of Negative Pressure	301
16.8 Conclusions	301
17 On the Interpretation of the Glass Transition in Terms of Fictive (Internal) Pressure and Fictive Temperature	
<i>Jürg W. P. Schmelzer⁽¹⁾ and Ivan Gutzow⁽²⁾</i>	
<i>(1) Institut für Physik, Universität Rostock, 18051 Rostock, Germany</i>	
<i>(2) Rostislav Kaischew Institute of Physical Chemistry, Bulgarian Academy of Sciences, 1113 Sofia, Bulgaria</i>	303
17.1 Introduction	303
17.2 Basic Thermodynamic Equations	303
17.3 Thermodynamic Properties	305
17.4 Fictive (Internal) Pressure as the Structural Order Parameter	309
17.4.1 Definition and Consequences	309
17.4.2 Some Further Topics of Discussion	310
17.5 On Some Recent Attempts of Re-Introduction of Fictive Temperatures into the Thermodynamics of the Glassy State	313
17.6 Model-Independent Definition of Fictive (Internal) Pressure and Fictive Temperature	315
18 Cluster Dynamics Simulation of Mixed Cu-Vacancy Clusters in Neutron-irradiated Fe-Cu Alloys	
<i>Alexander R. Gokhman⁽¹⁾ and Frank Bergner⁽²⁾</i>	
<i>(1) South Ukraine Pedagogical University, Staroportofrankovskaya 26, 65020 Odessa, Ukraine</i>	
<i>(2) Forschungszentrum Dresden - Rossendorf, Postfach 510119, 01314 Dresden, Germany</i>	319
18.1 Introduction	319
18.2 Irradiation Conditions	320
18.3 Study of the Iron-Copper-Vacancy System in Neutron Irradiated Model Alloy B	320
18.4 Conclusion	325
19 Formation of Nano - Size Condensed States in Amorphous - Crystal Silicon Multi-Interface Structures	
<i>(1) V. P. Yefimov, A. S. Abyzov, A. N. Dovbnya, V. V. Slezov, A. V. Rybka, V. V. Zakutin, N. G. Reshetnyak, A. A. Blinkin, E. P. Bereznyak, V. S. Demin, V. P. Romasko, (2) Yu. E. Gordienko, S. V. Babychenko, and G. N. Bendeberya</i>	
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<i>(2) Kharkov National University of Radioelectronics, Lenin Avenue 14, Kharkov, 61166, Ukraine</i>	327
19.1 Introduction	327

19.2 Model of Lateral Amorphous-Crystal Structures in the (c-Si)-Semiconductor of p-Type	330
19.3 Influence of Dimensional Effects on the Optical and Electric Properties of the Interface Structures	331
19.4 Irradiation Technique	333
19.5 Investigation of Electric Parameters at the Surface of the Samples	336
19.6 IR-absorption Spectra	341
19.7 Conclusions	341
20 Nonlinear Fast Relaxation of Coexisting Short and Lengthy Micelles	
<i>Mikhail S. Kshevetskiy and Alexander K. Shchekin</i>	
<i>Department of Statistical Physics, St. Petersburg State University, Ulyanovskaya st. 1, Petrodvorets, 198 504 St. Petersburg, Russia</i>	343
20.1 Introduction	343
20.2 Kinetic Equation of Micellization and Quasi-equilibrium Distributions	344
20.3 Moment Equations for Short Micelles	345
20.4 Moment Equations for Lengthy Micelles	348
20.5 Solution of the Moment Equations for the Short Micelles	350
20.6 Solution of the Moment Equations for the Lengthy Micelles	351
20.7 Solution of the Moment Equations for Coexisting Short and Lengthy Micelles	353
20.8 Conclusions	354
21 Deliquescence and Efflorescence Barriers in Heterogeneous Nucleation in Undersaturated Vapor	
<i>Alexander K. Shchekin and Ilya V. Shabaev</i>	
<i>Department of Statistical Physics, St. Petersburg State University, Ulyanovskaya st. 1, Petrodvorets, 198 504 St. Petersburg, Russia</i>	357
21.1 Introduction	357
21.2 Two-dimensional Surface of the Work of Droplet Formation	358
21.3 Well and Saddle Points of the Work of Droplet Formation at Partial Dissolution of the Nucleus	360
21.4 Stable and Unstable Variables of the Droplet State	365
22 On Bose-Einstein Condensation in a Weakly Interacting Bose Gas	
<i>Alexander L. Tseskis</i>	
<i>Am Weidenbusch 29, 51381 Leverkusen, Germany</i>	369
22.1 Introduction	369
22.2 Critical Temperature and LEH at $D = 3$	370
22.3 BEC in a Non-ideal Weakly Interacting Bose Gas	372
22.4 Conclusions	376
23 On the Effect of Elastic Stresses on Crystallization Processes in Finite Domains	
<i>Alexander S. Abyzov⁽¹⁾, Jürg W. P. Schmelzer⁽²⁾, and Vladimir M. Fokin⁽³⁾</i>	
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23.1 Introduction	379
23.2 Systems with Spherical Geometry: Basic Equations	380
23.3 Determination of the Constants C_1 and C_2 for Different Cases	380
23.3.1 Deformation of a Sphere	380

25.2 Content of the Proceedings <i>Nucleation Theory and Applications</i> 1997-99, 2000-02, and 2003-05 and of the Monograph <i>Nucleation Theory and Applications</i> with Overview Lec- tures Published by WILEY-VCH in 2005	465
25.3 Monographs Published or Accepted by WILEY-VCH for Publication Prepared by Partici- pants of the Workshops	469
25.4 List of Participants	469