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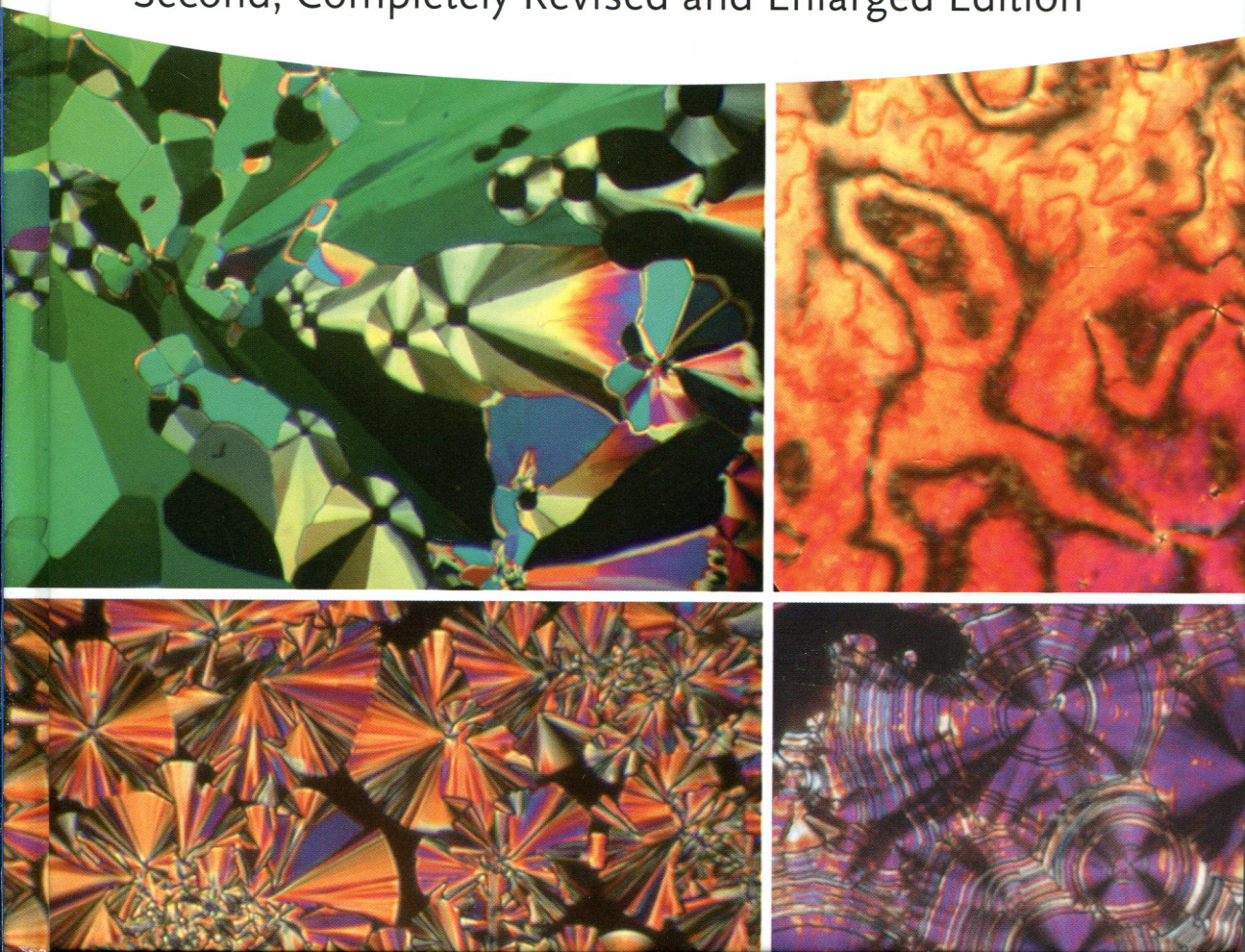
Edited by J.W. Goodby, P.J. Collings, T. Kato,
C. Tschierske, H.F. Gleeson, P. Raynes

Handbook of Liquid Crystals

Volume 2:
Physical Properties and Phase Behavior of Liquid Crystals

Second, Completely Revised and Enlarged Edition



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Volume 2: Physical Properties and Phase Behavior of Liquid Crystals

8 Volume Set: Second, completely revised and greatly enlarged edition

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