

Ekkehard Holzbecher

Environmental Modeling

Using MATLAB

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Environmental Modeling

Using MATLAB®

 Springer

Priv.-Doz. Dr.-Ing. Dipl.-Math. Ekkehard Holzbecher
Georg-August Universität Göttingen
Goldschmidtstr. 3
37077 Göttingen
eholzbe@gwdg.de

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Contents

Part I Primer to Modeling with MATLAB®

| | | |
|----------|---|-----------|
| 1 | Introduction | 3 |
| 1.1 | Environmental Modeling Using MATLAB® | 3 |
| 1.2 | Introduction to MATLAB® | 7 |
| 1.2.1 | Getting Started with MATLAB® | 8 |
| 1.2.2 | Matrices in MATLAB® | 15 |
| 1.2.3 | Basic Matrix Operations | 19 |
| 1.3 | A Simple Environmental Model | 25 |
| 1.4 | MATLAB® Graphics – The Figure Editor | 29 |
| 1.5 | MATLAB® Help System | 32 |
| | References | 32 |
| 2 | Fundamentals of Modeling, Principles and MATLAB® | 35 |
| 2.1 | Model Types | 35 |
| 2.2 | Modeling Steps | 36 |
| 2.3 | Fundamental Laws | 40 |
| 2.3.1 | Conservation of Mass | 40 |
| 2.3.2 | Conservation of Momentum | 41 |
| 2.3.3 | Conservation of Energy | 41 |
| 2.4 | Continuity Equation for Mass | 42 |
| 2.5 | MATLAB® M-files | 46 |
| 2.6 | Ifs and Loops in MATLAB® | 51 |
| 2.7 | Debugging of M-files | 55 |
| | Reference | 56 |
| 3 | Transport | 57 |
| 3.1 | The Conservation Principle | 57 |
| 3.2 | Fick’s Law and Generalizations | 59 |
| 3.2.1 | Diffusion | 59 |
| 3.2.2 | Dispersion | 63 |

| | | |
|----------|--|------------|
| 3.3 | The Transport Equation | 64 |
| 3.3.1 | Mass Transport | 64 |
| 3.3.2 | Fourier's Law and Heat Transport | 68 |
| 3.4 | Dimensionless Formulation | 71 |
| 3.5 | Boundary and Initial Conditions | 71 |
| | References | 73 |
| 4 | Transport Solutions | 75 |
| 4.1 | 1D Transient Solution for the Infinite Domain | 75 |
| 4.2 | A Simple Numerical Model | 80 |
| 4.3 | Comparison Between Analytical and Numerical Solution | 88 |
| 4.4 | Numerical Solution Using MATLAB® pdepe | 90 |
| 4.5 | Example: 1D Inflow Front | 93 |
| | References | 95 |
| 5 | Transport with Decay and Degradation | 97 |
| 5.1 | Decay and Degradation | 97 |
| 5.2 | 1D Steady State Solution | 100 |
| 5.3 | Dimensionless Formulation | 102 |
| 5.4 | Transient Solutions | 108 |
| | References | 110 |
| 6 | Transport and Sorption | 111 |
| 6.1 | Interphase Exchange | 111 |
| 6.2 | Retardation | 117 |
| 6.3 | Analytical Solution | 120 |
| 6.4 | Numerical Solutions | 122 |
| 6.5 | Slow Sorption | 126 |
| 6.6 | MATLAB® Animations | 130 |
| | References | 132 |
| 7 | Transport and Kinetics | 133 |
| 7.1 | Introduction | 133 |
| 7.2 | Law of Mass Action for Kinetic Reactions | 136 |
| 7.3 | Monod, Michaelis–Menten and Blackwell Kinetics | 137 |
| 7.4 | Bacteria Populations | 138 |
| 7.5 | Steady States | 140 |
| | References | 145 |
| 8 | Transport and Equilibrium Reactions | 147 |
| 8.1 | Introductory Example | 147 |
| 8.2 | The Law of Mass Action for Equilibrium Reactions | 151 |
| 8.3 | Speciation Calculations | 153 |
| 8.4 | Sorption and the Law of Mass Action | 157 |
| 8.5 | Transport and Speciation | 160 |
| | References | 166 |

| | | |
|--|---|-----|
| 9 | Ordinary Differential Equations: Dynamical Systems | 169 |
| 9.1 | Streeter-Phelps Model for River Purification | 170 |
| 9.2 | Details of Michaelis–Menten or Monod Kinetics | 173 |
| 9.3 | 1D Steady State Analytical Solution | 176 |
| 9.4 | Redox Sequences | 184 |
| | References | 188 |
| 10 | Parameter Estimation | 191 |
| 10.1 | Introduction | 191 |
| 10.2 | Polynomial Curve Fitting | 193 |
| 10.3 | Exponential Curve Fitting | 196 |
| 10.4 | Parameter Estimation with Derivatives | 198 |
| 10.5 | Transport Parameter Fitting | 206 |
| 10.6 | General Procedure | 209 |
| | References | 213 |
| Part II Advanced Modeling Using MATLAB® | | |
| 11 | Flow Modeling | 217 |
| 11.1 | The Navier-Stokes Equations for Free Fluids | 218 |
| 11.2 | The Euler Equations and the Bernoulli Theorem | 224 |
| 11.3 | Darcy’s Law for Flow in Porous Media | 228 |
| 11.4 | Flow in Unsaturated Porous Media | 232 |
| | References | 237 |
| 12 | Groundwater Drawdown by Pumping | 239 |
| 12.1 | Confined Aquifer | 239 |
| 12.2 | Unconfined Aquifer | 242 |
| 12.3 | Half-confined Aquifer | 245 |
| 12.4 | Unsteady Drawdown and Well Function | 246 |
| 12.5 | Automatic Transmissivity Estimation | 248 |
| | References | 252 |
| 13 | Aquifer Baseflow and 2D Meshing | 253 |
| 13.1 | 1D Analysis | 253 |
| 13.2 | 1D Implementation | 255 |
| 13.3 | 2D Implementation | 257 |
| 13.4 | Meshs and Grids | 260 |
| | Reference | 263 |
| 14 | Potential and Flow Visualization | 265 |
| 14.1 | Definition and First Examples | 265 |
| 14.2 | Potential and Real World Variables | 268 |
| 14.3 | Example: Groundwater Baseflow and Well | 270 |
| 14.4 | MATLAB® 2D Graphics | 273 |
| 14.5 | MATLAB® 3D Graphics | 278 |
| | References | 279 |

| | | |
|-----------|--|-----|
| 15 | Streamfunction and Complex Potential | 281 |
| 15.1 | Streamfunction | 281 |
| 15.2 | The Principle of Superposition | 285 |
| 15.2.1 | The Doublet | 286 |
| 15.2.2 | Mirror Wells | 287 |
| 15.3 | Complex Analysis and Complex Potential | 291 |
| 15.4 | Example: Vortices or Wells Systems | 295 |
| 15.5 | Example: Thin Objects in Potential Flow | 299 |
| | References | 301 |
| 16 | 2D and 3D Transport Solutions (Gaussian Puffs and Plumes) | 303 |
| 16.1 | Introduction | 303 |
| 16.2 | 2D Instantaneous Line Source | 308 |
| 16.3 | 2D Constant Line Source | 309 |
| 16.4 | 3D Instantaneous Source | 309 |
| 16.5 | 3D Constant Source | 311 |
| | References | 315 |
| 17 | Image Processing and Geo-Referencing | 317 |
| 17.1 | Introduction | 317 |
| 17.2 | Reading and Display | 318 |
| 17.3 | Geo-Referencing | 319 |
| 17.4 | Digitizing | 322 |
| 17.5 | MATLAB® Functions | 324 |
| | References | 325 |
| 18 | Compartment Graphs and Linear Systems | 327 |
| 18.1 | Compartments and Graphs | 327 |
| 18.2 | Linear Systems | 331 |
| 18.3 | Eigenvalues and Phase Space | 341 |
| | References | 346 |
| 19 | Nonlinear Systems | 347 |
| 19.1 | Logistic Growth | 347 |
| 19.2 | Competing Species | 350 |
| 19.3 | Predator–Prey Models | 356 |
| 19.4 | Chaos (Lorenz Attractor) | 360 |
| | References | 362 |
| 20 | Graphical User Interfaces | 363 |
| 20.1 | The MATLAB® Guide | 363 |
| 20.2 | The Transport GUI | 371 |
| | References | 375 |
| 21 | Numerical Methods: Finite Differences | 377 |
| 21.1 | Introductory Example | 378 |
| 21.2 | Finite Differences | 381 |
| 21.3 | A Finite Difference Example | 386 |

| | | |
|--------------------------------|--|------------|
| 21.4 | Solution for the 2D Poisson equation | 389 |
| 21.5 | Solution for the 2D Diffusion-Decay Equation | 392 |
| | References | 393 |
| Supplements | | 395 |
| | Supplement 1: MATLAB® Data Import | 395 |
| | Supplement 2: Data Export | 398 |
| | Supplement 3: Data Presentation in a Histogram | 398 |
| | Epilogue | 399 |
| | References | 400 |
| MATLAB1 Command Index | | 401 |
| Companion Software List | | 405 |
| Index | | 407 |